

III. Simple Regression.

- A. Introduction
- B. Population Regression Equation
- C. Sample Regression Equation
- D. Ordinary Least Squares
- E. Classical Regression Model.
- F. Properties of OLS Estimators (**BLUE**)
- G. Estimator for  $\sigma^2$
- H. **Inference** (we've done this before!)

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H. Inference in Simple Regression

1. Introduction:

*Inference:* Combine point estimates and *sampling distribution information.*

2.  $\sigma^2$  known

3.  $\sigma^2$  NOT known

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4. Hypothesis tests: Six Steps

**Step 1: Hypotheses.** Start with the *alternative* or *research hypothesis*.

*Tests for  $\beta_1$*  – what does theory suggest for the effect of X on Y? This determines your alternative hypothesis.

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Using your sample of 30 used 2004 Honda Accords, test the hypothesis we just stated.

Step 1: State the hypotheses:

Step 2: Choose the level of significance.

Step 3: Determine **critical value(s)**. Draw!

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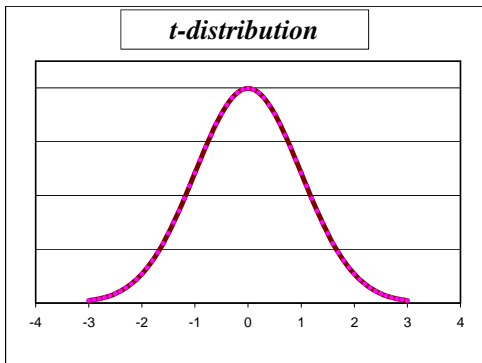
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**Step 4:** Draw your sample, estimate, determine the value for the standardized test statistic:

$$t_{calc} = \frac{\hat{\beta}_1 - \beta_1^0}{s_{\hat{\beta}_1}}$$

**PRS 4:** Using **your** regression results, **calculate the test statistic** for the hypothesis stated above. **Round to 3 decimal places.**

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Step 5: Compare – how do you make a decision?

**PRS 5:** Complete the hypothesis test:  
 $H_0: \beta_1 \geq 0$ ;  $H_a: \beta_1 < 0$ ,  
using **your sample** of 30 used 2004 Honda  
Accords. What is your conclusion?

**0. Reject  $H_0$ .**  
**1. Fail to Reject  $H_0$**

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Step 6: Conclusion.

**Fail to Reject:**

**Reject:**

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The true PRF for used 2004 Accords is:

$E[\text{Price} | \text{Miles}] = \$23,383.90 - \$0.0894 \text{ Miles}$

What is the appropriate test for a **true null hypothesis for the effect of mileage on price?**

Set up this test:

- (1) Hypothesis
- (2) Choose level of significance.
- (3) Determine critical values.

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