

III. Simple Regression.

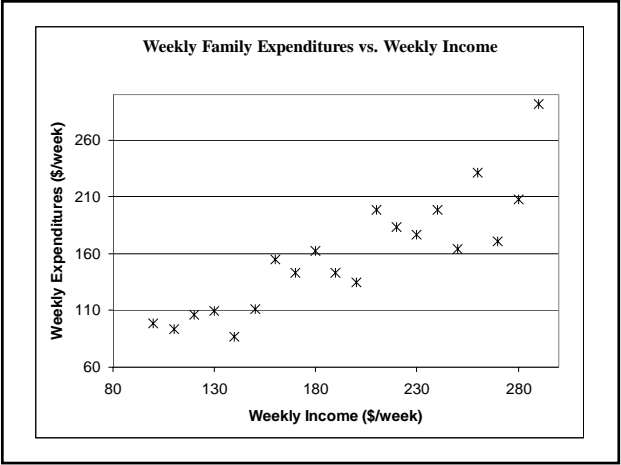
- A. Introduction
- B. Population Regression Equation
- C. Sample Regression Equation
- D. Ordinary Least Squares
- E. Classical Regression Model.
- F. Properties of OLS Estimators (**BLUE**)
- G. Estimator for σ^2
- H. Inference
- I. Goodness of Fit
- J. Forecasting or Prediction

I. Goodness of Fit

1. **Objective** – a summary statistic that tells us how well our model “fits the data.”
 - Estimators for $E[Y]$, we now have two. What are they?

2. Measures for the Dependent Variable:

- Y_i :
- \bar{Y} :
- \hat{Y}_i :



Decomposition in terms of distances (deviations):

- Total Deviation:
- Explained Deviation:
- Unexplained Deviation:

These deviations always add-up:

3. Sums of Squares

- We want to know how we did on average.
- But, summing deviations always gives zero.
- Square them! Then sum:

The Sums of Squared Deviations always add-up:

4. R^2 a measure of Goodness of Fit.

- What we have: $TSS = ESS + RSS$
- Form a ratio:
- Interpretation:
- Range of possible R^2 values:

J. Prediction or Forecasting

1. Predicting or Forecasting Population Values. (Estimation)

- What two population values for Y could we predict?

2. Estimators – what estimator do we have for each of these population values?

- Mean prediction: $E[Y | X_0] = \beta_0 + \beta_1 X_0$
- Estimator: $\hat{Y}_0 = \hat{\beta}_0 + \hat{\beta}_1 X_0$
- Standard Error: $s_{\hat{Y}_0} = \sqrt{\hat{\sigma}^2 \left[\frac{1}{n} + \frac{(X_0 - \bar{X})^2}{\sum x_i^2} \right]}$
- Individual Prediction: $Y | X_0 = \beta_0 + \beta_1 X_0 + u_0$
- Estimator: $\hat{Y}_0 = \hat{\beta}_0 + \hat{\beta}_1 X_0$

$$s_{Y_0} = \sqrt{\hat{\sigma}^2 \left[1 + \frac{1}{n} + \frac{(X_0 - \bar{X})^2}{\sum x_i^2} \right]}$$
